

Robust Beamforming for Secrecy Rate in Cooperative Cognitive Radio Multicast Communications

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Abstract—In this paper, we propose a cooperative approach to improve the security of both primary and secondary systems in cognitive radio multicast communications. During their access to the frequency spectrum licensed to the primary users, the secondary unlicensed users assist the primary system in fortifying security by sending a jamming noise to the eavesdroppers, while simultaneously protect themselves from eavesdropping. The main objective of this work is to maximize the secrecy rate of the secondary system, while adhering to all individual primary users' secrecy rate constraints. In the case of passive eavesdroppers and imperfect channel state information knowledge at the transceivers, the utility function of interest is nonconcave and involved constraints are nonconvex, and thus, the optimal solutions are troublesome. To address this problem, we propose an iterative algorithm to arrive at a local optimum of the considered problem. The proposed iterative algorithm is guaranteed to achieve a Karush-Kuhn-Tucker solution.

I. INTRODUCTION

Recently, physical layer (PHY) security for wireless communications has become an important research area. The underlying idea is to guarantee a positive secrecy rate of legitimate users by exploiting the random characteristics of the wireless channel. In particular, the authors in [1] proposed a low-complexity on/off power allocation strategy to attain secrecy under the assumption of full channel state information (CSI). The use of cooperative jamming noise (JN) was proposed in [2], where users who are prevented from transmitting according to a certain policy will block the eavesdropper and thereby assist the remaining users. From a quality-of-service perspective, a secret transmit beamforming approach was considered in [3], in order to predetermine the signal-to-interference-plus-noise-ratio (SINR) target at the destination and/or at the eavesdropper.

Being a critical issue, PHY security of cognitive radio networks (CRNs), which are faced with specific security risks due to the broadcasting nature of radio signals [4]–[6], however, has not been well investigated until recently, e.g., in [7]–[11]. More specifically, in [7] and [8], multi-antennas at the secondary transmitter were utilized to attain beamforming that maximizes the secrecy capacity of the secondary system, while adhering to the peak interference constraint at the primary receiver. Furthermore, a simple case

with single antenna at the eavesdropper was considered in [9]. In [10], the authors considered a CRN model, where both the primary user (PU) and the secondary user (SU) send their confidential messages to intended receivers that are surrounded by a single eavesdropper.

In this paper, we consider the PHY security in cooperative cognitive radio multicast communications, where the eavesdroppers intend to wiretap data from both the primary and secondary systems. We assume that the primary transmitter is equipped only with a single antenna, which implies that the primary transmitter cannot generate a jamming signal or design a beamforming vector to protect itself from the eavesdroppers. The secrecy capacity of the primary system is improved by implementing a cooperative framework between the primary and secondary systems. Specifically, the primary allows the secondary system to share its spectrum, and in return the secondary system sends jamming noise to degrade the eavesdropper's channel, in order to protect the primary system. Specifically, the main contributions of this paper can be summarized as follows:

- We design a joint information and jamming signal at the secondary transmitter, where information is intended for secondary receivers and jamming noise is intended for eavesdroppers. The main objective is to maximize the secrecy rate of the secondary system, while satisfying the minimum secrecy rate requirement for each legitimate user of the primary system as well as the power constraint.
- We propose a method to find the approximate solution for optimal transmit beamforming, by providing the convexity of the problem that is considered through the use of a convex approximation. The optimal solutions of transmit beamforming for the confidential information and jamming noise do not fix the transmit strategy.
- We provide extensive numerical results to justify the novelty of the proposed algorithm and compare its performance with the known solutions. In particular, the numerical results demonstrate fast convergence of the proposed algorithm and significantly improve the secrecy rate compared with the known solutions. We should

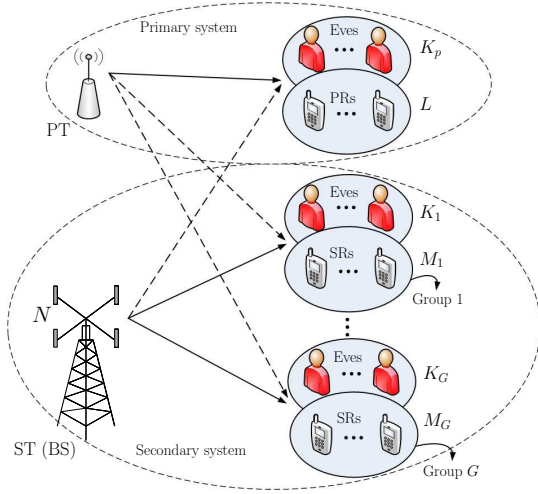


Figure 1. A cooperative CRN multicast transmission model with multiple eavesdroppers.

remark that our results are more general than in [10], which was considered under the assumptions of one eavesdropper and perfect CSI.

II. SYSTEM MODEL AND OPTIMIZATION PROBLEM

A. System Model

The primary system consists of one primary transmitter (PT) and L primary receivers (PRs), while the secondary system consists of one secondary transmitter (ST) and M secondary receivers (SRs), as illustrated in Fig. 1. The ST, which is a base station (BS), is equipped with N antennas, whereas all other nodes are equipped with only one antenna. The opportunistic spectrum access is improved by assigning the ST to send G information bearing signals $s_g, g = 1, \dots, G$, where s_g is the information being sent to the g -th group with unit average power $\mathbb{E}\{|s_g|^2\} = 1$. We assume that each individual multicast group \mathcal{G}_g in the secondary system consists of M_g the secondary receivers. Specifically, the number of SRs in group \mathcal{G}_g is denoted by $S_g = \{1, \dots, m_g, \dots, M_g\}$. Then, the total number of SRs in the secondary system with multicast transmission is indeed $M = \sum_{g=1}^G M_g$. Regarding security, we assume that the eavesdroppers (Eves) potentially intend to wiretap and decode confidential messages from both the primary and secondary systems [12]. We assume that each group \mathcal{G}_g and the PRs are respectively wiretapped by a set of Eves such as $\mathcal{K}_{e,g} \triangleq \{1, \dots, k_g, \dots, K_g\}, \forall g$ and $\mathcal{K}_p \triangleq \{1, \dots, k_p, \dots, K_p\}$. This implies that at the same time, each legitimate user is wiretapped by a separate group of Eves.

We aim to design multiple beamforming vectors at the ST, one for the JN and the other for its own information signal, to protect both the primary and secondary systems. The transmit power at the PT is $P_p > 0$ and the data intended for the PR is x_p with unit average power $\mathbb{E}\{|x_p|^2\} = 1$. Before transmission, the data of the SRs s_g in the group \mathcal{G}_g is weighted to the $N \times 1$ beamforming vector $\mathbf{w}_g, \forall g$. Hence, all the transmitted signals at the ST can be expressed through

a vector \mathbf{x}_s as

$$\mathbf{x}_s = \sum_{g=1}^G \mathbf{w}_g s_g + \mathbf{u} \quad (1)$$

where \mathbf{u} is the artificial noise vector, whose elements are zero-mean complex Gaussian random variables with covariance matrix $\mathbf{U}\mathbf{U}^H$, such that $\mathbf{u} \sim \mathcal{CN}(\mathbf{0}, \mathbf{U}\mathbf{U}^H)$, where $\mathbf{U} \in \mathbb{C}^{N \times N}$. The artificial noise \mathbf{u} is assumed to be unknown to all SRs, PRs, and Eves. For notational simplicity, we define $\mathbf{w} \triangleq [\mathbf{w}_1^T, \mathbf{w}_2^T, \dots, \mathbf{w}_G^T]^T \in \mathbb{C}^{NG \times 1}$.

The corresponding SINR at the l -th PR for $l = 1, \dots, L$ and the k_p -th Eve for $k_p = 1, \dots, K_p$ are respectively given by¹

$$\Gamma_{p,l}(\mathbf{w}, \mathbf{U}) = \frac{P_p |h_l|^2}{\sum_{g=1}^G |\mathbf{f}_l^H \mathbf{w}_g|^2 + \|\mathbf{f}_l^H \mathbf{U}\|^2 + \sigma_l^2} \quad (2)$$

$$\Gamma_{e,k_p}(\mathbf{w}, \mathbf{U}) = \frac{P_p |g_{k_p}|^2}{\sum_{g=1}^G |\mathbf{f}_{k_p}^H \mathbf{w}_g|^2 + \|\mathbf{f}_{k_p}^H \mathbf{U}\|^2 + \sigma_{k_p}^2} \quad (3)$$

where $h_l \in \mathbb{C}, g_{k_p} \in \mathbb{C}, \mathbf{f}_l \in \mathbb{C}^{N \times 1}$, and $\mathbf{f}_{k_p} \in \mathbb{C}^{N \times 1}$ are the respective baseband equivalent channels of the links PT \rightarrow l -th PR, PT \rightarrow k_p -th Eve, ST \rightarrow l -th PR, and ST \rightarrow k_p -th Eve. σ_l^2 and $\sigma_{k_p}^2$ are the variance of the additive white Gaussian noise (AWGN) at the l -th PR and k_p -th Eve, respectively.

The respective SINR at the m_g -th SR in the group \mathcal{G}_g and the k_g -th Eve are given by

$$\Gamma_{s,m_g}(\mathbf{w}, \mathbf{U}) = \frac{|\mathbf{h}_{m_g}^H \mathbf{w}_g|^2}{\sum_{i=1, i \neq g}^G |\mathbf{h}_{m_g}^H \mathbf{w}_i|^2 + \|\mathbf{h}_{m_g}^H \mathbf{U}\|^2 + P_p |f_{m_g}|^2 + \sigma_{m_g}^2} \quad (4)$$

$$\Gamma_{e,k_g}(\mathbf{w}, \mathbf{U}) = \frac{|\mathbf{g}_{k_g}^H \mathbf{w}_g|^2}{\sum_{i=1, i \neq g}^G |\mathbf{g}_{k_g}^H \mathbf{w}_i|^2 + \|\mathbf{g}_{k_g}^H \mathbf{U}\|^2 + P_p |f_{k_g}|^2 + \sigma_{k_g}^2} \quad (5)$$

where $\mathbf{h}_{m_g} \in \mathbb{C}^{N \times 1}, \mathbf{g}_{k_g} \in \mathbb{C}^{N \times 1}, f_{m_g} \in \mathbb{C}$, and $f_{k_g} \in \mathbb{C}$ are the corresponding baseband equivalent channels of the links ST \rightarrow m_g -th SR, ST \rightarrow k_g -th Eve, PT \rightarrow m_g -th SR, PT \rightarrow k_g -th Eve. $\sigma_{m_g}^2$ and $\sigma_{k_g}^2$ are the variance of AWGN at the m_g -th PR and k_g -th Eve, respectively.

The achievable secrecy rate for the l -th PR of the primary system, denoted by $C_{p,l}(\mathbf{w}, \mathbf{U})$, can be expressed as [1]

$$C_{p,l}(\mathbf{w}, \mathbf{U}) = \left[\log_2(1 + \Gamma_{p,l}(\mathbf{w}, \mathbf{U})) - \max_{k_p \in \mathcal{K}_p} \log_2(1 + \Gamma_{e,k_p}(\mathbf{w}, \mathbf{U})) \right]^+ \quad (6)$$

where $[x]^+ = \max\{0, x\}$. The achievable secrecy rate for the m_g -th SR of the secondary system, denoted by $C_{s,m_g}(\mathbf{w}, \mathbf{U})$, can be expressed as [1]

$$C_{s,m_g}(\mathbf{w}, \mathbf{U}) = \left[\log_2(1 + \Gamma_{s,m_g}(\mathbf{w}, \mathbf{U})) - \max_{k_g \in \mathcal{K}_{e,g}} \log_2(1 + \Gamma_{e,k_g}(\mathbf{w}, \mathbf{U})) \right]^+ \quad (7)$$

¹ $\|\cdot\|$ and $|\cdot|$ denote the Euclidean norm of a matrix or vector and the magnitude of a complex scalar, respectively.

B. Optimization Problem Formulation

The objective of the system design is to maximize the minimum (max-min) secrecy rate of the secondary system while satisfying the minimum quality-of-service (QoS) requirements, such as the secrecy rate achievable for the primary system as follows

$$\text{P.1 : } \max_{\mathbf{w}, \mathbf{U}} \min_{m_g \in \mathcal{S}_g, g \in \mathcal{G}} C_{s,m_g}(\mathbf{w}, \mathbf{U}) \quad (8a)$$

$$\text{s. t. } C_{p,l}(\mathbf{w}, \mathbf{U}) \geq \bar{R}_{p,l}, l \in \mathcal{L} \quad (8b)$$

$$\sum_{g=1}^G \|\mathbf{w}_g\|^2 + \|\mathbf{U}\|^2 \leq P_s \quad (8c)$$

where $\mathcal{L} \triangleq \{1, \dots, L\}$ and $\mathcal{G} \triangleq \{1, \dots, G\}$. In (8b), $\bar{R}_{p,l} > 0$ are the minimum secrecy rate requirement for each legitimate user of the primary system.

C. CSI Model

We consider a realistic scenario, where the instantaneous CSI between ST and PRs is imperfect and Eves are passive. Specifically, the CSI of the link between the ST and PRs is given as [13]

$$\begin{aligned} \mathbf{f}_l &= \hat{\mathbf{f}}_l + \Delta \mathbf{f}_l, \forall l \\ \Omega_l &\triangleq \{\Delta \mathbf{f}_l \in \mathbb{C}^{N \times 1} : \Delta \mathbf{f}_l^H \Delta \mathbf{f}_l \leq \delta_l^2\} \end{aligned} \quad (9)$$

where $\hat{\mathbf{f}}_l$ is the channel estimate of the l -th PR available at the ST, and $\Delta \mathbf{f}_l$ represents the associated CSI error. For notational simplicity, we define Ω_l as a set of all possible CSI errors associated with the l -th PR. We assume that $\Delta \mathbf{f}_l$ are deterministic and bounded, and therefore δ_l represents the size of the uncertainty region of the estimated CSI of the l -th PR.

For the passive Eves, we further assume that the entries of g_{k_p} , \mathbf{f}_{k_p} , $\forall k_p$, f_{k_g} , and \mathbf{g}_{k_g} , $\forall k_g$, follow independent and identically distributed (i.i.d.) Rayleigh fading, and that the instantaneous CSI of these wiretap channels is not available at ST. These assumptions of passive Eves are commonly used in the literature [9], [13], [14]. Meanwhile, the channels \mathbf{h}_{m_g} , $\forall m, g$, are assumed to be perfectly known since the SRs are active users in the secondary system.

III. PROPOSED SOLUTION

In this section, we propose an iterative algorithm that arrives a local optimum of the considered optimization problem. As the first step, we convert (8) to another equivalent form as

$$\text{maximize } \min_{\mathbf{w}, \mathbf{U}, t, z} \min_{m_g \in \mathcal{S}_g, g \in \mathcal{G}} \{\log_2(1 + \Gamma_{s,m_g}(\mathbf{w}, \mathbf{U})) - t_g\} \quad (10a)$$

$$\text{s. t. } \log_2(1 + \Gamma_{e,k_g}(\mathbf{w}, \mathbf{U})) \leq t_g, k_g \in \mathcal{K}_{e,g}, g \in \mathcal{G} \quad (10b)$$

$$\log_2(1 + \Gamma_{p,l}(\mathbf{w}, \mathbf{U})) - z \geq \bar{R}_{p,l}, l \in \mathcal{L} \quad (10c)$$

$$\log_2(1 + \Gamma_{e,k_p}(\mathbf{w}, \mathbf{U})) \leq z, k_p \in \mathcal{K}_p \quad (10d)$$

$$(8c) \quad (10e)$$

where $t \triangleq \{t_g\}$ and z are the maximum allowable rate for Eve to wiretap the information from the ST and PT, respectively. The equivalence of (8) and (10) can be easily confirmed by justifying that the constraint (10b) must hold with equality at optimum.

Based on the above setting and the assumptions in Section II. C, the optimization problem P.1 can be reformulated as

$$\text{P.2 : } \text{maximize } \varphi \quad (11a)$$

$$\text{s. t. } \log_2(1 + \Gamma_{s,m_g}(\mathbf{w}, \mathbf{U})) - t_g \geq \varphi, \forall m_g, \forall g \quad (11b)$$

$$\max_{\mathbf{g}_{k_g}, f_{k_g}} \log_2(1 + \Gamma_{e,k_g}(\mathbf{w}, \mathbf{U})) \leq t_g, \forall k_g, \forall g \quad (11c)$$

$$\min_{\Delta \mathbf{f}_l \in \Omega_l} \log_2(1 + \Gamma_{p,l}(\mathbf{w}, \mathbf{U})) - z \geq \bar{R}_{p,l}, \forall l \quad (11d)$$

$$\max_{\mathbf{g}_{k_p}, f_{k_p}} \log_2(1 + \Gamma_{e,k_p}(\mathbf{w}, \mathbf{U})) \leq z, \forall k_p \quad (11e)$$

$$(8c). \quad (11f)$$

where φ is newly introduced variable. Observe that the objective function is monotonic in its argument, therefore, we now only deal with the nonconvex constraints (11b)-(11e). Let us treat the constraint (11b) first. As the first step, (4) is equivalently rewritten by

$$\Gamma_{s,m_g}(\mathbf{w}, \mathbf{U}) = \frac{|\mathbf{h}_{m_g}^H \mathbf{w}_g|^2}{\chi_{s,m_g}(\mathbf{w}, \mathbf{U})} \quad (12)$$

where

$$\chi_{s,m_g}(\mathbf{w}, \mathbf{U}) = \sum_{i=1, i \neq g}^G |\mathbf{h}_{m_g}^H \mathbf{w}_i|^2 + \|\mathbf{h}_{m_g}^H \mathbf{U}\|^2 + P_p |f_{m_g}|^2 + \sigma_{m_g}^2.$$

From (12), it follows that

$$\begin{aligned} \ln\left(1 + \frac{|\mathbf{h}_{m_g}^H \mathbf{w}_g|^2}{\chi_{s,m_g}(\mathbf{w}, \mathbf{U})}\right) \\ = -\ln\left(1 - \frac{|\mathbf{h}_{m_g}^H \mathbf{w}_g|^2}{\chi_{s,m_g}(\mathbf{w}, \mathbf{U}) + |\mathbf{h}_{m_g}^H \mathbf{w}_g|^2}\right). \end{aligned} \quad (13)$$

From the fact that $0 \leq \frac{|\mathbf{h}_{m_g}^H \mathbf{w}_g|^2}{\chi_{s,m_g}(\mathbf{w}, \mathbf{U}) + |\mathbf{h}_{m_g}^H \mathbf{w}_g|^2} \triangleq \Phi(\mathbf{w}, \mathbf{U}) < 1$, the function $-\ln(1 - \Phi(\mathbf{w}, \mathbf{U}))$ is jointly convex w.r.t. the involved variables [15], which is useful for developing an approximate solution for (13). In particular, at feasible point $(\mathbf{w}^{(n)}, \mathbf{U}^{(n)})$, we have²

$$\begin{aligned} -\ln\left(1 - \frac{|\mathbf{h}_{m_g}^H \mathbf{w}_g|^2}{\chi_{s,m_g}(\mathbf{w}, \mathbf{U}) + |\mathbf{h}_{m_g}^H \mathbf{w}_g|^2}\right) &\geq \\ -\ln\left(1 - \frac{|\mathbf{h}_{m_g}^H \mathbf{w}_g^{(n)}|^2}{\chi_{s,m_g}(\mathbf{w}^{(n)}, \mathbf{U}^{(n)}) + |\mathbf{h}_{m_g}^H \mathbf{w}_g^{(n)}|^2}\right) & \\ -\Gamma_{s,m_g}(\mathbf{w}^{(n)}, \mathbf{U}^{(n)}) + 2 \frac{\Re\{(\mathbf{w}_g^{(n)})^H \mathbf{h}_{m_g} \mathbf{h}_{m_g}^H \mathbf{w}_g\}}{\chi_{s,m_g}(\mathbf{w}^{(n)}, \mathbf{U}^{(n)})} & \\ - \frac{\Gamma_{s,m_g}(\mathbf{w}^{(n)}, \mathbf{U}^{(n)}) (\chi_{s,m_g}(\mathbf{w}, \mathbf{U}) + |\mathbf{h}_{m_g}^H \mathbf{w}_g|^2)}{(\chi_{s,m_g}(\mathbf{w}^{(n)}, \mathbf{U}^{(n)}) + |\mathbf{h}_{m_g}^H \mathbf{w}_g^{(n)}|^2)} & \\ := \mathcal{F}_{m_g}^{(n)}(\mathbf{w}, \mathbf{U}). & \end{aligned} \quad (14)$$

Note that $\mathcal{F}_{m_g}^{(n)}(\mathbf{w}, \mathbf{U})$ is convex and is global lower bound of $-\ln(1 - \Phi(\mathbf{w}, \mathbf{U}))$. Therefore, the following equality holds

²Hereafter, suppose the value of (\mathbf{w}, \mathbf{U}) at the $(n+1)$ -th iteration in an iterative algorithm presented shortly is denoted by $(\mathbf{w}^{(n)}, \mathbf{U}^{(n)})$.

at optimum

$$\mathcal{F}_{m_g}^{(n)}(\mathbf{w}^{(n)}, \mathbf{U}^{(n)}) = -\ln\left(1 - \frac{|\mathbf{h}_{m_g}^H \mathbf{w}_g^{(n)}|^2}{\chi_{s,m_g}(\mathbf{w}^{(n)}, \mathbf{U}^{(n)}) + |\mathbf{h}_{m_g}^H \mathbf{w}_g^{(n)}|^2}\right). \quad (15)$$

It implies that we can iteratively replace $-\ln(1 - \Phi(\mathbf{w}, \mathbf{U}))$ by $\mathcal{F}_{m_g}^{(n)}(\mathbf{w}^{(n)}, \mathbf{U}^{(n)})$ to achieve a convex approximation of (11b) [16]. Hence, by substituting (12), (13), and (14) to (11b), we have

$$\mathcal{F}_{m_g}^{(n)}(\mathbf{w}, \mathbf{U}) \geq (\varphi + t_g) \ln 2. \quad (16)$$

It is now clear that the difficulty in solving (11) is due to (11c)-(11e) since the remaining constraints are convex and approximate convex. Instead of this, we can find a sub-optimal solution of (11) as follows

$$\underset{\mathbf{w}, \mathbf{U}, t, z, \varphi, \phi, \alpha, \beta}{\text{maximize}} \quad \varphi \quad (17a)$$

$$\text{s. t. } \log_2(1 + \phi_g) \leq t_g, \quad g \in \mathcal{G} \quad (17b)$$

$$\Pr\left(\max_{k_g \in \mathcal{K}_{e,g}} \Gamma_{e,k_g}(\mathbf{w}, \mathbf{U}) \leq \phi_g\right) \geq \epsilon_g, \quad g \in \mathcal{G} \quad (17c)$$

$$\log_2(1 + \alpha_l) - z \geq \bar{R}_{p,l}, \quad l \in \mathcal{L} \quad (17d)$$

$$\min_{\Delta \mathbf{f}_l \in \Omega_l} \Gamma_{p,l}(\mathbf{w}, \mathbf{U}) \geq \alpha_l, \quad l \in \mathcal{L} \quad (17e)$$

$$\log_2(1 + \beta) \leq z \quad (17f)$$

$$\Pr\left(\max_{k_p \in \mathcal{K}_p} \Gamma_{e,k_p}(\mathbf{w}, \mathbf{U}) \leq \beta\right) \geq \tilde{\epsilon} \quad (17g)$$

$$(8c), (11b) \quad (17h)$$

where $\phi = \{\phi_g\}$, $\alpha = \{\alpha_l\}$, and β are newly introduced variables. The constraint (17e) is imposed to ensure that for a given CSI error set Ω_l , the minimum received SINR at the l -th PR is larger than the minimum SINR requirement α_l for the PR. According to (17c) and (17g), the probabilities that the maximum received SINR at the k_g -th passive Eve and at the k_p -th Eve are less than $\phi_g > 0$ and $\beta > 0$ are ensured to be greater than ϵ_g and $\tilde{\epsilon}$, respectively.

We are now in position to expose the hidden convexity of the constraint of (17c), (17e), and (17g). Since \mathbf{U} does not require a rank-constraint matrix, we introduce $\tilde{\mathbf{U}} \triangleq \mathbf{U}\mathbf{U}^H$ to facilitate the optimization problem. Let us handle the constraint (17e) first by rewriting as

$$\max_{\Delta \mathbf{f}_l \in \Omega_l} \sum_{g=1}^G |\mathbf{f}_l^H \mathbf{w}_g|^2 + \text{tr}(\mathbf{f}_l^H \tilde{\mathbf{U}} \mathbf{f}_l) + \sigma_l^2 \leq \frac{P_p |h_l|^2}{\alpha_l}. \quad (18)$$

For arbitrary l -th PR, (18) can be shaped to take the following equivalent form

$$\sum_{g=1}^G \mu_{l,g} + \tilde{\mu}_l + \sigma_l^2 \leq \frac{P_p |h_l|^2}{\alpha_l}, \quad l \in \mathcal{L} \quad (19)$$

$$\max_{\Delta \mathbf{f}_l \in \Omega_l} |\mathbf{f}_l^H \mathbf{w}_g|^2 \leq \mu_{l,g}, \quad l \in \mathcal{L}, g \in \mathcal{G} \quad (20)$$

$$\max_{\Delta \mathbf{f}_l \in \Omega_l} \text{tr}(\mathbf{f}_l^H \tilde{\mathbf{U}} \mathbf{f}_l) \leq \tilde{\mu}_l, \quad l \in \mathcal{L} \quad (21)$$

where $\mu_l = \{\mu_{l,g}\}$ and $\tilde{\mu} = \{\tilde{\mu}_l\}$ are new variables. Note that both sides of (19) are convex, so it is iteratively replaced by

the following linear constraint

$$\sum_{g=1}^G \mu_{l,g} + \tilde{\mu}_l + \sigma_l^2 \leq \frac{2P_p |h_l|^2}{\alpha_l^{(n)}} - \frac{P_p |h_l|^2}{(\alpha_l^{(n)})^2} \alpha_l, \quad l \in \mathcal{L}. \quad (22)$$

To make the tractable form of (20) and (21), we first transform these constraints into a matrix inequality. Substituting $\mathbf{f}_l = \hat{\mathbf{f}}_l + \Delta \mathbf{f}_l, \forall l$ into (20) and applying *S-Procedure* [15], then

$$\begin{aligned} \Delta \mathbf{f}_l^H \Delta \mathbf{f}_l - \delta_l^2 &\leq 0 \\ \Rightarrow (20) : \Delta \mathbf{f}_l^H \mathbf{w}_g \mathbf{w}_g^H \Delta \mathbf{f}_l + 2\Re\{\hat{\mathbf{f}}_l^H \mathbf{w}_g \mathbf{w}_g^H \Delta \mathbf{f}_l\} \\ &\quad + \hat{\mathbf{f}}_l^H \mathbf{w}_g \mathbf{w}_g^H \hat{\mathbf{f}}_l - \mu_{l,g} \leq 0 \end{aligned} \quad (23)$$

holds if and only if there exists $\omega_l = \{\omega_{l,g} \geq 0\}, \forall l$, so that the matrix inequality constraint holds as

$$\begin{bmatrix} \omega_{l,g} \mathbf{I}_N - \mathbf{w}_g \mathbf{w}_g^H & -\mathbf{w}_g \mathbf{w}_g^H \hat{\mathbf{f}}_l \\ -\hat{\mathbf{f}}_l^H \mathbf{w}_g \mathbf{w}_g^H & -\hat{\mathbf{f}}_l^H \mathbf{w}_g \mathbf{w}_g^H \hat{\mathbf{f}}_l - \omega_{l,g} \delta_l^2 + \mu_{l,g} \end{bmatrix} \succeq \mathbf{0}. \quad (24)$$

However, (24) is still not in a tractable form. At this point, we apply the application of Schur's complement lemma [17, Eq. (7.2.6)] to obtain the following linear matrix inequality (LMI)

$$\begin{aligned} \exists \omega_{l,g} \geq 0 : \mathbf{C}_{l,g}(\mathbf{w}_g, \mu_{l,g}, \omega_{l,g}) &\triangleq \\ \begin{bmatrix} 1 & \mathbf{w}_g^H & -\mathbf{w}_g^H \hat{\mathbf{f}}_l \\ \mathbf{w}_g & \omega_{l,g} \mathbf{I}_N & \\ -\hat{\mathbf{f}}_l^H \mathbf{w}_g & & -\omega_{l,g} \delta_l^2 + \mu_{l,g} \end{bmatrix} &\succeq \mathbf{0}, \quad g \in \mathcal{G}, l \in \mathcal{L}. \end{aligned} \quad (25)$$

It is also worth noting that constraint (25) now includes only a finite number of constraints.

Analogously, with $\tilde{\omega} = \{\tilde{\omega}_l \geq 0\}$, the constraint (21) admits the following representation

$$\begin{aligned} \exists \tilde{\omega}_l \geq 0 : \tilde{\mathbf{C}}_l(\tilde{\mathbf{U}}, \tilde{\mu}_l, \tilde{\omega}_l) &\triangleq \\ \begin{bmatrix} \tilde{\omega}_l \mathbf{I}_N - \tilde{\mathbf{U}} & -\tilde{\mathbf{U}} \hat{\mathbf{f}}_l \\ -\hat{\mathbf{f}}_l^H \tilde{\mathbf{U}} & -\hat{\mathbf{f}}_l^H \tilde{\mathbf{U}} \hat{\mathbf{f}}_l - \tilde{\omega}_l \delta_l^2 + \tilde{\mu}_l \end{bmatrix} &\succeq \mathbf{0}, \quad l \in \mathcal{L}. \end{aligned} \quad (26)$$

To deal with the nonconvex constraints given in (17g) and (17c), we provide the following two lemmas, whose proofs are omitted due to space limitations.

Lemma 1: For the primary system, the constraint in (17g) is lower bounded by the following constraint

$$\lambda_{\min} \left(\sum_{g=1}^G \mathbf{w}_g \mathbf{w}_g^H + \tilde{\mathbf{U}} \right) \geq \tilde{\xi}(\beta) \quad (27)$$

where $\tilde{\xi}(\beta) \triangleq \left(\exp\left(-\frac{\beta}{N P_p} \sigma_{k_p}^2\right) / (1 - \tilde{\epsilon}^{1/K_p})^{1/N} - 1 \right) \frac{P_p}{\beta}$ and $\lambda_{\min}(\mathbf{X})$ denotes the minimum eigenvalue of matrix \mathbf{X} .

Next, we rewrite (27) equivalently in the form of

$$2 \ln \eta + \beta \frac{\sigma_{k_p}^2}{N P_p} \geq 0 \quad (28)$$

$$(\eta^2 / (1 - \tilde{\epsilon}^{1/K_p})^{1/N} - 1) P_p \leq \beta \theta \quad (29)$$

$$\lambda_{\min} \left(\sum_{g=1}^G \mathbf{w}_g \mathbf{w}_g^H + \tilde{\mathbf{U}} \right) \geq \theta \quad (30)$$

where θ and η are newly introduced variables. We now focus on the nonconvex constraint. For the nonconvex constraint (30), we note that both $\sum_{g=1}^G \mathbf{w}_g \mathbf{w}_g^H$ and $\tilde{\mathbf{U}}$ are Hermitian matrices. In addition, the eigenvalues of a Hermitian matrix

\mathbf{Q} are real and satisfy $\text{tr}(\mathbf{x}^H \mathbf{Q} \mathbf{x}) \geq \lambda \|\mathbf{x}\|^2$ for any given vector \mathbf{x} if and only if $\lambda_{\min}(\mathbf{Q}) \geq \lambda$. Since $\lambda_{\min}(\mathbf{w}_g \mathbf{w}_g^H) = 0$ for all g , the lower bound of right side of (30) is given by

$$\lambda_{\min}\left(\sum_{g=1}^G \mathbf{w}_g \mathbf{w}_g^H + \tilde{\mathbf{U}}\right) \geq \lambda_{\min}(\tilde{\mathbf{U}}). \quad (31)$$

From (30), it follows that

$$\lambda_{\min}(\tilde{\mathbf{U}}) \geq \theta \Leftrightarrow \tilde{\mathbf{U}} \succeq \mathbf{I}_N \theta. \quad (32)$$

Lemma 2: For the secondary system, the constraint in (17c) is lower bounded by the following constraint

$$\frac{\|\mathbf{w}_g\|^2}{\phi_g} \leq \xi_g + \sum_{i=1, i \neq g}^G \|\mathbf{w}_i\|^2 + \lambda_{\min}(\tilde{\mathbf{U}}), \quad g \in \mathcal{G} \quad (33)$$

where $\xi_g \triangleq \left[\exp\left(\frac{\sigma_{k_g}^2}{N P_p}\right) \epsilon_g^{-1/N K_g} - 1 \right] P_p$.

The formulation in (33) can be further shaped to take the following convex constraints

$$\frac{\|\mathbf{w}_g\|^2}{\phi_g} \leq \xi_g + \sum_{i=1, i \neq g}^G 2\Re\{(\mathbf{w}_i^{(n)})^H \mathbf{w}_i\} - \sum_{i=1, i \neq g}^G \|\mathbf{w}_i^{(n)}\|^2 + \vartheta, \quad g \in \mathcal{G} \quad (34)$$

$$\lambda_{\min}(\tilde{\mathbf{U}}) \geq \vartheta \Leftrightarrow \tilde{\mathbf{U}} \succeq \mathbf{I}_N \vartheta \quad (35)$$

where ϑ is newly introduced variable.

With the above discussions, the approximate convex problem solved at $(n+1)$ -th iteration of the proposed design is given by

$$\begin{aligned} & \underset{\substack{\mathbf{w}, \tilde{\mathbf{U}} \succeq \mathbf{0}, \mathbf{t}, z, \varphi, \phi, \alpha, \\ \beta, \mu_l, \tilde{\mu}_l, \omega_l, \tilde{\omega}_l, \theta, \eta, \vartheta}}{\text{maximize}} \quad \varphi \end{aligned} \quad (36a)$$

$$\text{s. t.} \quad \mathcal{F}_{m_g}^{(n)}(\mathbf{w}, \tilde{\mathbf{U}}) \geq (\varphi + t_g) \ln 2, \quad m_g \in \mathcal{S}_g, g \in \mathcal{G} \quad (36b)$$

$$\sum_{g=1}^G \|\mathbf{w}_g\|^2 + \text{tr}(\tilde{\mathbf{U}}) \leq P_s \quad (36c)$$

$$(17b), (17d), (17f), (22), (25),$$

$$(26), (28), (29), (32), (34), (35). \quad (36d)$$

To find an initial feasible point to (11), we solve the following convex optimization problem

$$\begin{aligned} & \underset{\substack{\mathbf{w}, \tilde{\mathbf{U}} \succeq \mathbf{0}, z, \alpha, \beta, \\ \mu_l, \tilde{\mu}_l, \omega_l, \tilde{\omega}_l, \theta, \eta}}{\text{max}} \quad \min_{l \in \mathcal{L}} \left\{ \log_2(1 + \alpha_l) - z - \bar{R}_{p,l} \right\} \end{aligned} \quad (37a)$$

$$\text{s. t.} \quad (17f), (22), (25), (26), (28), (29), (32), (36c) \quad (37b)$$

and stop at reaching: $\min_{l \in \mathcal{L}} \left\{ \log_2(1 + \alpha_l) - z - \bar{R}_{p,l} \right\} \geq 0$.

The proposed iterative method is outlined in Algorithm 1. We can show that Algorithm 1 yields a nondecreasing sequence of the objective value due to updating the involved variables after each iteration, which converges to a KKT point [16].

Complexity Analysis: The optimization problem in (36) involves GL LMI constraints of size $N+2$, L LMI constraints of size $N+1$, and 2 LMI constraints of size N . In each iteration of Algorithm 1, the worst-case computational complexity for solving the generic convex problem in (36) using interior point methods is given by $\mathcal{O}\left(n\sqrt{GL(N+2) + L(N+1) + 2N}[GL(N+2)^3 + L(N+1)^3 + 2N^3 + nGL(N+2)^2 + nL(N+1)^2 + 2nN^2 + n^2]\right)$, where $n = G(L+3) + N(N+G) + 2L + 6$ [18].

Algorithm 1 The proposed iterative algorithm to solve (11)

Initialization: Set $n := 0$ and solve (37) to generate an initial feasible point $(\mathbf{w}^{(n)}, \tilde{\mathbf{U}}^{(n)}, \alpha^{(n)})$

1: **repeat**

2: Solve (36) to obtain the optimal solution: $(\mathbf{w}^*, \tilde{\mathbf{U}}^*, \alpha^*)$.

3: Update $\mathbf{w}^{(n+1)} := \mathbf{w}^*$, $\tilde{\mathbf{U}}^{(n+1)} := \tilde{\mathbf{U}}^*$, and $\alpha^{(n+1)} := \alpha^*$.

4: Set $n := n + 1$.

5: **until** Convergence or maximum required number of iterations

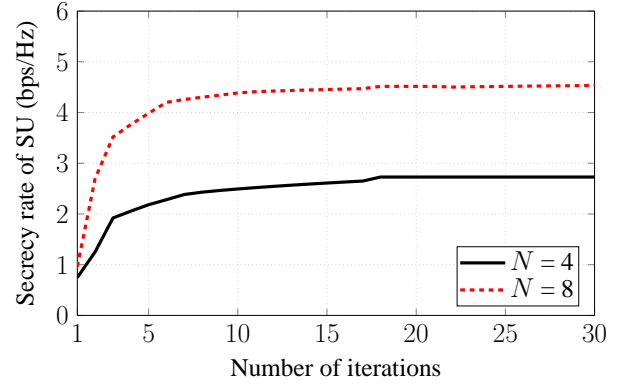


Figure 2. Convergence results of Algorithm 1 for different numbers of antennas at the ST over one random channel realization with $\bar{R}_p = 2$ bps/Hz and $P_s = 15$ dBm.

IV. NUMERICAL RESULTS AND DISCUSSIONS

The number of groups of SUs is set to $G = 2$, each of which consists of two SR users, i.e., $M_g = 2, \forall g$. The number of PR is set to $L = 2$, and each group of SUs and PUs is surrounded by two Eves, i.e., $K_p = K_g = 2$. All channel entries are assumed to be i.i.d. complex Gaussian random variables with $\mathcal{CN}(0, 1)$, and the background thermal noise at each user is generated as i.i.d. complex Gaussian random variables with zero means and unit variance. The transmit power at the PT is fixed to $P_p = 20$ dBm. For simplicity, we further assume that the minimum secrecy rate requirement for all PUs are the same, i.e., $\bar{R}_{p,l} = \bar{R}_p, \forall l$. For the imperfect CSI of the PU channels, we define the normalized channel estimation errors as $\delta_l^2 = \delta_l^2 / \|\mathbf{f}_l\|^2 = 5\%, \forall l$. To guarantee secure communications, we choose $\tilde{\epsilon} = 0.99$ and $\epsilon_g = 0.99, \forall g$ for the passive Eves.

Fig. 2 illustrates the typical convergence behavior of the proposed Algorithm 1. As seen, the objective value of the proposed algorithm increases rapidly within the first 10 iterations and stabilize after a few more iterations, and its convergence rate is slightly sensitive to the problem size i.e., as N increases. The convergence results also confirm that all optimization variables are accounted to find a better solution for the next iteration, i.e., the secrecy rates of SUs monotonically increasing.

We compare the performance of the proposed scheme with the known solutions, namely the “No JN scheme” [8] and “JN-aided scheme (non-robust)”. In “No JN scheme”, we set \mathbf{U} to $\mathbf{0}$. For the non-robust secrecy rate design, we use the

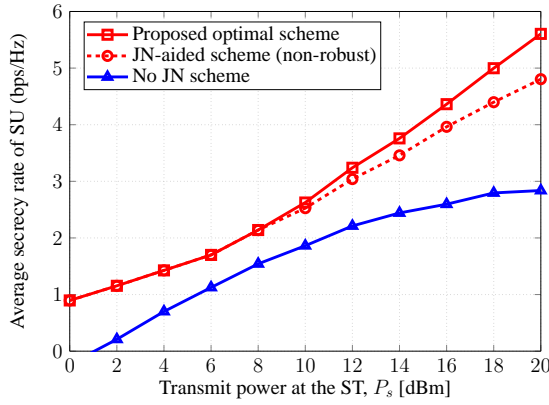


Figure 3. Average secrecy rate of the secondary system vs. the transmit power at the ST, where $\bar{R}_p = 1$ bps/Hz and $N = 8$.

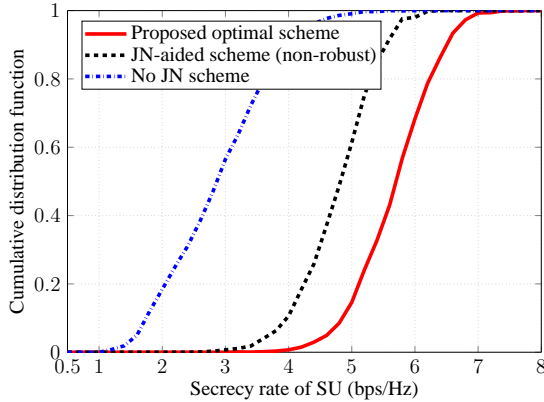


Figure 4. CDF of secrecy rate of the secondary system for different schemes, where $\bar{R}_p = 1$ bps/Hz, $N = 8$, and $P_s = 20$ dBm.

presumed CSIs as \hat{f}_l , $\forall l$ rather than the true ones, to perform the transmit design, which then evaluates the resultant secrecy rate. Fig. 3 depicts the secrecy rate as a function of the transmit power at the ST. As can be observed that the secrecy rate of non-robust design is sensitive to the CSI uncertainties for high P_s . In particular, when $P_s \geq 8$ dBm, the non-robust design exhibits the degradation in terms of the secrecy rate that tends to worsen as P_s increases. Moreover, the proposed optimal design achieves the best secrecy rate performance, compared to the other designs.

Finally, we generate cumulative distribution function (CDF) of the secrecy rate of the secondary system in Fig. 4 for different schemes. It is obvious in CDF that on account for a larger feasible set, the proposed optimal scheme can promise a bigger secrecy rate as expected. For instance, the proposed optimal scheme attains 0.8 bps/Hz and 2.8 bps/Hz of the achievable secrecy rate higher than the non-robust scheme and “No JN scheme”, respectively, for approximately 60% of the simulated trials.

V. CONCLUSION

In this paper, we have proposed PHY security for both primary and secondary systems in the presence of the multiple secondary receiver groups and multiple primary receivers. The main objective is to maximize the secrecy rate of the secondary system, while the secondary transmitter is constrained not

only by power constraint, but also by the individual the minimum secrecy rate requirements of the primary users. We have proposed iterative algorithms to solve the optimization problem based on a convex formulation in each iteration. We have carried out simulation to evaluate the advantages of the proposed design.

ACKNOWLEDGMENT

This work was supported in part by the U.K. Royal Academy of Engineering Research Fellowship under Grant RF1415\14\22 and U.K. Engineering and Physical Sciences Research Council under Grant EP/P019374/1.

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